

Instructions: Show all of your work... No credit will be given for illegible or illogical work, or for final answers that are not justified by the work shown. Place all final answers in the spaces provided. This exam is **closed book**. You may find the following formulas helpful during this exam:

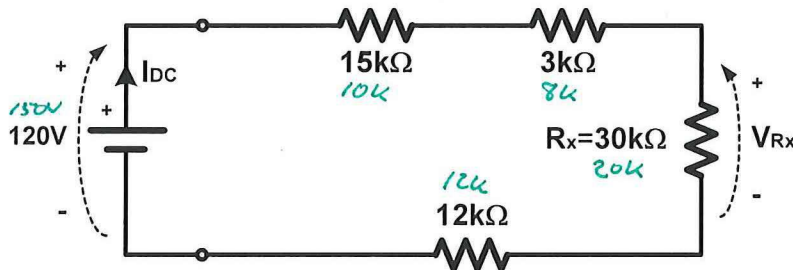
$$V = I \cdot R \quad R_{EQseries} = R_1 + R_2 + \dots + R_N \quad \text{KVL: } \sum V_{Rises} - \sum V_{Drops} = 0 \quad V_X = V_{total} \cdot \left(\frac{R_X}{R_{EQseries}} \right)$$

(around a closed loop)

$$P = V \cdot I \quad R_{EQparallel} = \left[\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N} \right]^{-1} \quad \text{KCL: } \sum I_{Entering} - \sum I_{Exiting} = 0 \quad I_X = I_{total} \cdot \left(\frac{R_{EQparallel}}{R_X} \right)$$

(a specific node)

16 Problem #1) Given the following circuit:



Determine:

- the total resistance $R_{EQseries}$ “seen” by the voltage source,
- the magnitude of the current I_{DC} that will flow out of the voltage source,
- the total electric power, P_{DC} , produced by the voltage source, and
- the electric power, P_{Rx} , consumed by resistor R_x .

$$R_{eq} = 15k + 3k + 30k + 12k = \boxed{60k\Omega}$$

$$I_{DC} = \frac{120V}{R_{eq}} = \frac{120V}{60,000} = \boxed{0.002A}$$

$$P_{DC} = V_{DC} \cdot I_{DC} = (120V)(0.002A) = \boxed{0.24W}$$

$$V_{Rx} = I_{Rx} \cdot R_x = (0.002A)(30,000\Omega) = 60V$$

$$P_{Rx} = V_{Rx} \cdot I_{Rx} = (60V)(0.002A) = \boxed{0.12W}$$

$$R_{eq} = 10 + 8 + 20 + 12 = \boxed{50k\Omega}$$

$$I_{DC} = \frac{150V}{50,000} = \boxed{0.003A}$$

$$P_{DC} = (150)(0.003) = \boxed{0.45W}$$

$$V_x = (0.003)(20000) = 60V$$

$$P_x = (60V)(0.003A) = \boxed{0.18W}$$

$R_{EQseries} =$	60	50	(kΩ)
$I_{DC} =$	0.002	0.003	(A)
$P_{DC} =$	0.24	0.45	(W)
$P_{Rx} =$	0.12	0.18	(W)

4 Problem #2) Determine the voltage V_{Rx} as shown in the above circuit using a voltage divider equation:

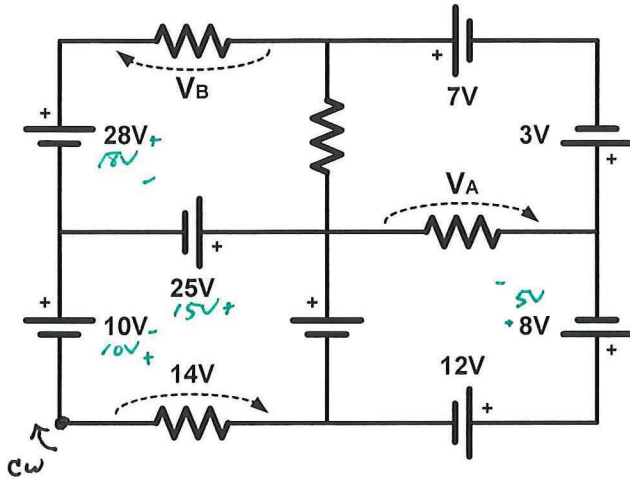
$$V_{Rx} = V_{DC} \left(\frac{R_x}{R_{eq}} \right) = 120 \left(\frac{30k}{60k} \right) = \boxed{60V}$$

$$V_x = 150 \left(\frac{20k}{50k} \right) = \boxed{60V}$$

You must show work utilizing a voltage divider equation to receive credit for part (c).

$$V_{Rx} = \underline{\quad 60 \quad} (V)$$

10 Problem #3) Use Kirchhoff's Voltage Law (KVL) to determine the voltage-rises V_A and V_B as defined in the following circuit.



You must completely write out the KVL equations that you utilized to solve V_A and V_B to receive credit for problem. (Show all of the terms in the equations)

Note that, although some voltages are intentionally not shown, you are provided with enough information to solve the required voltages.

$$A: -10 + 15 + V_A + 5 - 12 - 14 = 0$$

$$V_A + 16 = 0 \rightarrow V_A = \boxed{16V}$$

$$B: -10 + 18 - V_B - 7 + 3 + 5 - 12 - 14 = 0$$

$$-V_B - 17 = 0 \rightarrow V_B = \boxed{-17V}$$

$$A: 10 + 25 + V_A + 8 - 12 - 14 = 0$$

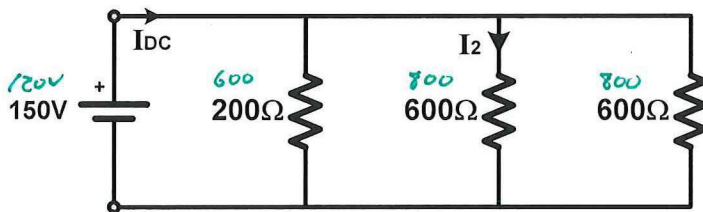
$$V_A + 17 = 0 \rightarrow V_A = \boxed{-17V}$$

$$B: 10 + 28 - V_B - 7 + 3 + 8 - 12 - 14 = 0$$

$$16 - V_B = 0 \rightarrow V_B = \boxed{16V}$$

$V_A =$	-17	16	(V)
$V_B =$	16	-17	(V)

12 Problem #4) Given the following circuit:



You must show work utilizing a current divider equation to receive credit for part (c).

Determine:

- the total resistance $R_{EQparallel}$ "seen" by the voltage source,
- the magnitude of the current I_{dc} that will flow out of the voltage source,
- the current I_2 as shown in the figure using a current divider equation,

$$R_{eq} = \left(\frac{1}{200} + \frac{1}{600} + \frac{1}{800} \right)^{-1} = (0.008\bar{3})^{-1} = \boxed{120\Omega}$$

$$R_{eq} = \left(\frac{1}{600} + \frac{1}{800} + \frac{1}{800} \right)^{-1} = (0.0041\bar{6})^{-1} = \boxed{240\Omega}$$

$$I_{dc} = \frac{150V}{R_{eq}} = \frac{150V}{120\Omega} = \boxed{1.25A}$$

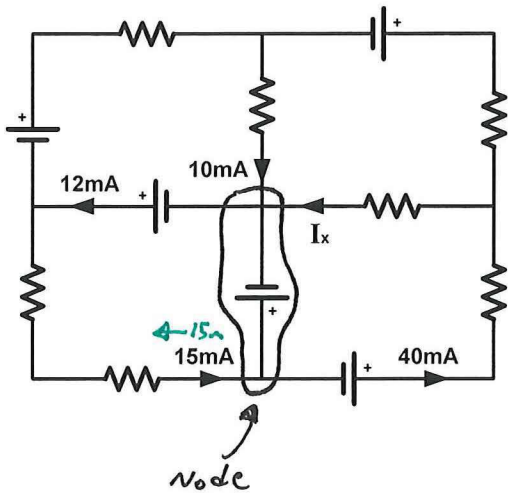
$$I_{dc} = \frac{120V}{240} = \boxed{0.5A}$$

$$I_2 = (0.5) \left(\frac{240}{800} \right) = (0.5)(0.3) = \boxed{0.15A}$$

$$I_2 = I_{dc} \left(\frac{R_{eq}}{R_2} \right) = (1.25) \left(\frac{120}{600} \right) = \boxed{0.25A}$$

$R_{EQparallel} =$	120	240	(Ω)
$I_{dc} =$	1.25	0.5	(A)
$I_2 =$	0.25	0.15	(A)

6 Problem #5) Determine the current I_x as defined in the circuit using Kirchhoff's Current Law.



You must completely write out the KCL equation(s) that you utilized to solve I_x to receive credit for problem.
(Show all of the terms in the equations)

Note that, although many currents are intentionally not shown, you are provided with enough information to solve the required current.

$$10\text{mA} + I_x = 12\text{mA} + 15\text{mA} + 40\text{mA}$$

$$10\text{mA} + I_x = 67\text{mA}$$

$$I_x = \boxed{57\text{mA}}$$

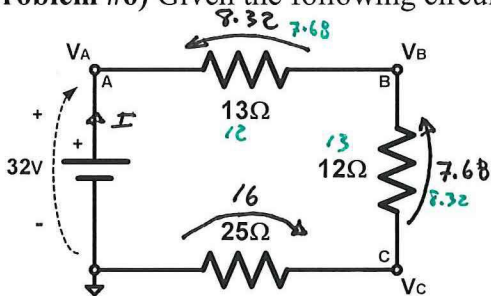
$$10\text{mA} + 15\text{mA} + I_x = 12\text{mA} + 40\text{mA}$$

$$25\text{mA} + I_x = 52\text{mA}$$

$$I_x = \boxed{27\text{mA}}$$

$$I_x = \underline{27} \mid \underline{57} \text{ (mA)}$$

18 Problem #6) Given the following circuit:



- Determine the **node voltages** V_A , V_B , and V_C in the circuit.
- If an ideal wire is connected from node **B** to node **C**, determine the new **node voltages** V_A , V_B , and V_C .

$$I = \frac{32}{13+12+25} = \frac{32}{50} = 0.64\text{A}$$

$$V_A = 0 + 32 = \boxed{32\text{V}}$$

$$V_B = V_A - 8.32 = \boxed{23.68\text{V}}$$

$$V_C = V_B - 7.68 = \boxed{16\text{V}}$$

$$I = 0.64$$

$$V_A = \boxed{32\text{V}}$$

$$V_B = 32 - 7.68 = \boxed{24.32\text{V}}$$

$$V_C = V_B - 8.32 = \boxed{16\text{V}}$$

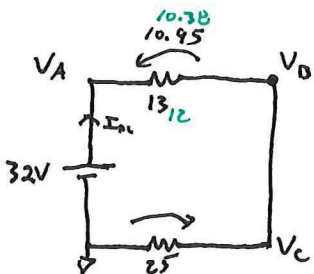
$$I_{bc} = \frac{32}{37} = 0.865\text{A}$$

$$V_A = \boxed{32\text{V}}$$

$$V_B = 32 - 10.38 = \boxed{21.62\text{V}}$$

$$V_C = V_B = \boxed{21.62\text{V}}$$

if resistor voltages -10V instead of node voltages!



$$I_{bc} = \frac{32}{13+25} = \frac{32}{38} = 0.842\text{A}$$

$$V_A = \boxed{32\text{V}}$$

$$V_B = V_A - 10.95 = \boxed{21.05\text{V}}$$

$$V_C = V_B = \boxed{21.05\text{V}}$$

a)	$V_A = 32$	32	(V)
	$V_B = 23.68$	24.32	(V)
	$V_C = 16$	16	(V)
b)	$V_A = 32$	32	(V)
	$V_B = 21.05$	21.62	(V)
	$V_C = 21.05$	21.62	(V)

14) Problem 7) Specify whether each of the statements are TRUE or FALSE.

- TRUE ~~TRUE~~ false Given a circuit that contains a single voltage source connected to multiple resistors, *electrons* will actually flow "out of" the positive terminal of the voltage source.
- TRUE ~~TRUE~~ false If two resistors are connected in *parallel* with each other in an active circuit, then the two resistors will have the same magnitude current flowing through them.
- TRUE ~~TRUE~~ TRUE If an *ideal wire* is connected across the same two nodes to which a resistor is connected, then no current will flow through the resistor.
- false ~~TRUE~~ TRUE If an *ideal wire* is connected across the same two nodes to which a resistor is connected, then there will be zero voltage across the resistor.
- false ~~TRUE~~ TRUE Based to *Kirchhoff's Voltage Law*, if all of the voltage-rises are defined in the clockwise direction around a closed-loop path, then at least one of the voltages must be negative.
- false ~~TRUE~~ false The *parallel equivalent resistance* of a set of parallel-connected resistors must be greater than the value of the smallest resistor in the set.
- TRUE ~~TRUE~~ TRUE Resistors convert electrical energy into heat.

60 kΩ
9.002 A
0.24 W

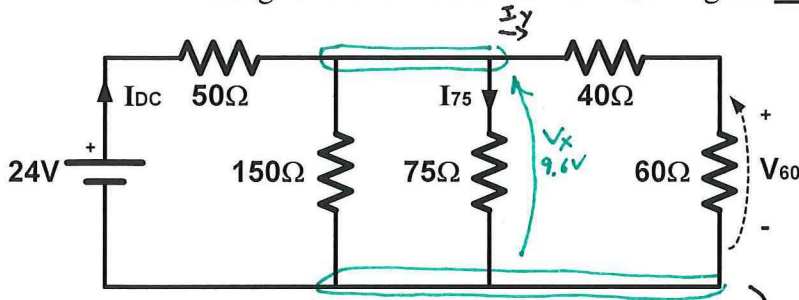
60kΩ 0.002A 0.24W 0.12W	60W	-17V 16V	120Ω 1.25A 0.25A	27mA	32V 23.68V 16V 32V 21.05V 21.05V	T/P	0.288A 0.128A 5.76V
50kΩ 0.003A 0.45W 0.18W		16V -17V	240Ω 0.5A 0.15A	57mA	32V 24.32V 16V 32V 21.62V 21.62V		

Do Not Write Below This Line

- 1) 16 2) 4 3) 10 4) 12 5) 6 6) 18 7) 14 8) 20 Total) _____

20

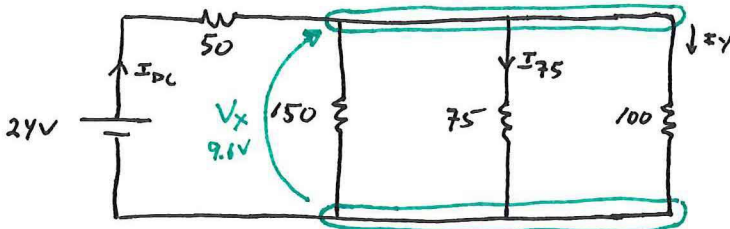
Problem #8) Determine the source current I_{DC} , the current flowing through the 75Ω resistor I_{75} , and the voltage across the 60Ω resistor V_{60} using the Reduce and Return Method.



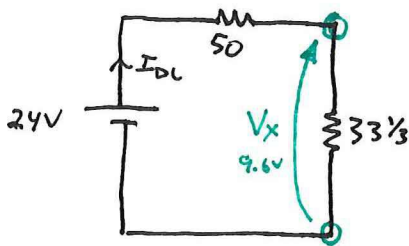
You must show work utilizing the Reduce and Return Method to receive credit for this problem.
Each time that you "reduce" the circuit, completely draw the reduced circuit and fully label all relevant circuit parameters.

$R_{eq} = 40 + 60 = 100 \Omega$

$V_{60} \equiv V_X = 9.6V$



$R_{eq} = \left(\frac{1}{150} + \frac{1}{75} + \frac{1}{100} \right)^{-1} = (0.03)^{-1} = 33\frac{1}{3} \Omega$



$I_{DC} = \frac{24V}{50 + 33\frac{1}{3}} = \frac{24V}{83\frac{1}{3}} = \underline{0.288 A}$

$V_X = I_{DC} \cdot (33\frac{1}{3}) = (0.288)(33\frac{1}{3}) = 9.6V$ or $V_X = 24 \left(\frac{33\frac{1}{3}}{83\frac{1}{3}} \right) = \underline{9.6V}$

$I_{75} = \frac{V_X}{75} = \frac{9.6V}{75\Omega} = \underline{0.128 A}$

or $I_{75} = 0.288 \left(\frac{33\frac{1}{3}}{75} \right) = \underline{0.128 A}$

$V_{60} = V_X \left(\frac{60}{40+60} \right) = (9.6V) \left(\frac{60\Omega}{100\Omega} \right) = \underline{5.76 V}$

or $I_Y = \frac{V_X}{100} = 0.096 A$
 $V_{60} = I_Y \cdot 60 = \underline{5.76 V}$

$I_{DC} = \underline{0.288} \text{ (A)}$

$I_{75} = \underline{0.128} \text{ (A)}$

$V_{60} = \underline{5.76} \text{ (V)}$